

An information-theoretic approach to estimating the composite genetic effects contributing to variation among generation means: Moving beyond the joint-scaling test for line cross analysis

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The pace and direction of evolution in response to selection, drift, and mutation are governed by the genetic architecture that underlies trait variation. Consequently, much of evolutionary theory is predicated on assumptions about whether genes can be considered to act in isolation, or in the context of their genetic background. Evolutionary biologists have disagreed, sometimes heatedly, over which assumptions best describe evolution in nature. Methods for estimating genetic architectures that favor simpler (i.e., additive) models contribute to this debate. Here we address one important source of bias, model selection in line cross analysis (LCA). LCA estimates genetic parameters conditional on the best model chosen from a vast model space using relatively few line means. Current LCA approaches often favor simple models and ignore uncertainty in model choice. To address these issues we introduce Software for Analysis of Genetic Architecture (SAGA), which comprehensively assesses the potential model space, quantifies model selection uncertainty, and uses model weighted averaging to accurately estimate composite genetic effects. Using simulated data and previously published LCA studies, we demonstrate the utility of SAGA to more accurately define the components of complex genetic architectures, and show that traditional approaches have underestimated the importance of epistasis.

KEY WORDS: Composite genetic effects, epistasis, genetic architecture, joint-scaling test, line cross analysis.

The genetic architecture of a trait is a description of how variation in genotypes map onto variation in phenotypes. Because the details of this mapping govern how a trait will respond to evolutionary forces, much of evolutionary theory is predicated on assumptions about whether genetic architectures are simple or complex (reviewed in Wolf et al. 2000; Svensson and Calsbeek 2012). As most textbooks will report, simple architectures, in which all genetic variation is due to additive gene action (i.e., heterozygotes have exactly intermediate value to either homozygote), provide the most efficient substrate for adaptation via natural selection (Fisher 1941; Crow and Kimura 1970; Lande and Arnold 1983; Lynch and Walsh 1998). However, more complex architectures that include within and between locus interactions (dominance and epistasis, respectively) can cause the available additive genetic variance to increase or decrease, and thereby accelerate or impede adaptation, even in the absence of additive gene action at any constituent locus (Goodnight 1988, 2000; Falconer and Mackay 1996, p. 128; Wade 2000, 2002; Carter et al. 2005; Carlborg et al. 2006). Genetic interactions may also facilitate evolutionary phenomena such as the origin of sex and recombination (Charlesworth 1990; Barton 1995; Peters and Lively 1999), mating system evolution (Charlesworth and Charlesworth 1990; Schierup and Christiansen 1996; Jacobs and Wade 2003), reproductive isolation (Cabot et al. 1994; Orr and Turelli 2001; Demuth and Wade 2005; Moehring et al. 2006), and developmental robustness and canalization (Rice 1998; Bergman and Siegal 2003; de Visser et al. 2003; Flatt 2005; Félix and Barkoulas 2015) that are each difficult to explain with theory that omits epistasis from the genetic architecture. There is also a broad correlation in evolutionary theory in which simpler architectures are emphasized when trait variation is among individuals within a family or population, but more complex architectures are emphasized as the relatedness among potential mates decreases (Lynch 1991; Coyne et al. 1997; Orr 2001; Demuth and Wade 2005). More specifically, inbreeding depression and heterosis between closely related individuals are traditionally attributed to dominance effects (Bruce 1910; Crow 1948; Lande and Schemske 1985; Charlesworth and Charlesworth 1999; but see Moorad and Wade 2005), a view consistent with observations of linear relationship between inbreeding and decline in trait mean (reviewed in Lynch and Walsh 1998; Byers and Waller 1999). In contrast, outcrossing depression and speciation are typically attributed to the breakup of coadapted gene complexes, environment-dependent effects (Carson and Templeton 1984; Fenster and Galloway 2000) and/or negative interactions between loci (Dobzhansky 1937; Muller 1940, 1942; Gavrilets 1997, 2003).

Debate over the relative importance of simple vs. complex architectures in nature has persisted among evolutionary biologists for decades (Wright 1931; Fisher 1958; Coyne et al. 1997; Wade and Goodnight 1998). It has been argued that reconciling the long-standing debates about when complex genetic interactions are important considerations for our understanding of evolution requires relevant empirical measures of genetic architecture along a continuum of divergence (Lynch 1991; Demuth and Wade 2005, 2006). However, efforts to empirically measure genetic architectures are often laborious and suffer from methodological biases against finding gene interactions (Demuth and Wade 2006). Our purpose in the work presented below is to alleviate a major source of bias associated with the line cross analysis approach to measuring genetic architecture.

Line cross analysis (LCA) is a widely used quantitative genetics method for estimating genetic architecture by partitioning a set of mean phenotypes into their composite genetic effects (CGEs; e.g., additive, dominance, and epistatic gene action). Originally developed in efforts to understand the genetic architecture of traits important to human agriculture (Mather and Jinks 1982), LCA has also provided insights into the genetic basis of adaptation and speciation (Armbruster et al. 1997; Lair et al. 1997; Edmands 1999; Galloway and Fenster 2001; Miller et al. 2003; Demuth and Wade 2005, 2007a,b; Tymchuk et al. 2007; Fuller 2008; Demuth et al. 2014). The LCA approach typically uses two parental strains that have diverged in a phenotype of interest. These parents are crossed, producing an F1, and subsequent crosses (e.g., F2, backcross, reciprocals) are made to generate groups that have different combinations of parental genes. We refer to each of these groups as cohorts. Using a weighted least squares regression with weights inversely proportional to the variance of the cohort means, the degree to which a phenotype is determined by different CGEs may be estimated (Cavalli 1952; Hayman 1958). It is important to keep in mind that LCA does not identify specific genetic features; rather CGEs represent the net effect of all genetic features contributing to the differences in the phenotype of interest between the parental lines. Furthermore, because LCA requires multiple generations, any environmental factors that contribute to spurious covariances among cohort means have the potential to confound estimates of genetic architecture. Failure to inter-randomize the cohorts in experimental assays may be an important source of faulty inference and deserves close attention during experimental design.

The most widely implemented statistical approach to testing among LCA models with different CGEs is called the joint-scaling (J-S) test (essentially a forward variable selection weighted least squares regression). Using this approach a simple additive model is first fit and then additional higher order CGEs are added until, based on the results of a likelihood ratio test, no significant improvement in the model is achieved (Mather and Jinks 1982; Lynch and Walsh 1998). This approach is common in studies of both plants and animals (Edmands 1999; Schiffer et al. 2006; van Heerwaarden et al. 2008; Bentz et al. 2011). Due to concerns that this approach may not find the best model, a number of alternative variable selection approaches have been implemented including backward and stepwise variable selection (Gilchrist and Partridge 1999; Demuth and Wade 2007 b). Additionally, hybrid approaches have been implemented using Akaike information criterion (AIC) to choose a most parsimonious model from an a priori chosen subset of potential models followed by the use of significance tests to add or remove CGEs and arrive at a final "best" model (Bieri and Kawecki 2003; Fritz et al. 2006; Fox et al. 2011). Finally, an iterative approach using AIC to compare multiple small candidate sets of models has been used to choose a single "best" model (Fox et al. 2004).

There are several documented issues with the variable selection processes implemented in the J-S test and existing ad hoc approaches (Whittingham et al. 2006): (1) Different variable selection approaches (forward, backward, and stepwise) do not consistently identify the same variables as important (Derksen and Keselman 1992). (2) Parameter estimates under these approaches are biased away from zero (Burnham and Anderson 2002). (3) Calculating valid *P*-values is difficult due to multiple comparisons (Wilkinson 1979). (4) Hypothesis testing approaches place an inappropriate focus on a single model ignoring the degree of model uncertainty implied by the data (Burnham and Anderson 2002). Finally, because the number of cohorts is often small relative to the number of CGEs being considered, the use of AIC as a metric is inappropriate for line cross data and should be replaced with AICc (Hurvich and Tsai 1989). More broadly, the often repeated aphorism that "all models are wrong, but some are useful" suggests that the search for a single best model may often be misguided (Box and Draper 1987). A more prudent approach would be to evaluate all models that the data allow and identify the useful one(s).

Following, we describe and demonstrate a full informationtheoretic (I-T) approach to model selection and parameter estimation for LCA that alleviates the difficulties associated with previous approaches and provides additional understanding that is not possible under a J-S, hybrid, or ad hoc approach. Our approach leverages the finite sample size corrected version of the Akaike information criterion (AICc) to explore all possible models and make unbiased and, when appropriate, model-averaged estimates of the contribution of CGEs to cohort means. We have developed an R package: Software for the Analysis of Genetic Architecture (SAGA) that makes this approach straightforward to implement. The SAGA software is available from the R package repository CRAN. We describe our approach and its performance on simulated datasets as well as contrasting the results of this method to those from the J-S test using 22 previously published datasets.

Method and Interpretation

The first step in LCA is the development of a C-matrix that describes the potential contribution of CGEs to cohort means. Two versions of C-matrices have been widely used and have been shown to have a linear relationship (Basford and De Lacy 1979). We use a C-matrix that is scaled to the midparent mean (equivalent to F_{∞}), and includes 23 potential CGEs (Table S1). By maximizing the number of CGEs (many of which are normally not explored), we reduce the risk that results are biased by the selection of CGEs tested. For each CGE we have calculated coefficients for 24 potential crosses; each of which is divided into male, female, or mixed sex cohorts.

Depending on the identity of the cohorts supplied, some CGEs may not vary or may be perfectly correlated with one another. Therefore, the first step in our approach is to reduce the C-matrix to include only the CGEs that can be partitioned with the available cohorts. Next, we generate all possible models that have at most two fewer CGEs than the number of cohorts being analyzed (number of cohorts—intercept—1). We use the existing implementation of weighted least squares regression in the base R package in the function GLM (R Development Core Team 2013). Some CGEs may be either highly correlated or contain a linear dependency (when one CGE can be described as a linear combination of one or more other CGEs). The GLM function will drop the highest order CGE from a model if it is highly correlated with a lower order CGE or if its inclusion creates a linear dependency. When this occurs it would effectively create a duplicate lower order model in the set being evaluated. If this occurs, we remove the equation with the confounded CGEs from the set being evaluated allowing the CGEs to be estimated independently by lower order equations that are otherwise equivalent.

The function GLM returns the parameter and standard error estimates conditional on the model as well as the AIC value for the model. AIC scores have been used to evaluate LCA models (Bieri and Kawecki 2003; Fox et al. 2004, 2011), but if the ratio of the number of cohorts to the number of CGEs being evaluated is less than 40, which will almost always be the case in LCA, then AICc is preferable (Burnham and Andersen 1998). AICc provides an appropriate trade-off between model complexity and goodness of fit, and as sample size increases it converges on AIC (McQuarrie and Tsai 1998). The higher penalty assessed for additional parameters under AICc should help to reduce the risk of including spurious variables and overfitting. We convert AIC to AICc using equation (1), where n is the number of cohorts and K is the number of parameters being estimated.

$$AICc = AIC + \frac{2K(K+1)}{n-K-1}$$
(1)

Once all models have been evaluated, we calculate AICc differences (Δ AICc) using equation (2).

$$\Delta \text{AICc}_i = \text{AICc}_i - \text{AICc}_{min}, \qquad (2)$$

where AICc_{min} is the minimum AICc score calculated across all possible models and AICc_i is the AICc calculated for a specific model. Δ AICc allows models to be ranked and is used in generating Akaike weights (w_i) using equation (3). The denominator in equation (3) is the summation of the numerator across all possible models being evaluated (R). The w_i generated in this way will sum to 1 and can be evaluated as evidence for whether a model is correct.

$$w_i = \frac{e^{-0.5 \times \Delta \text{AICc}_i}}{\sum_{r=1}^{R} e^{-0.5 \times \Delta \text{AICc}_r}}$$
(3)

If w_i of the best model is 0.95 or greater, then we perform parameter estimation under a single model. If no model reaches this threshold, then we construct a 95% confidence set of models that contains the minimum number of models whose w_i sum to 0.95. We then compute model-averaged results for the 95% confidence set. To calculate model-averaged parameter estimates and unconditional standard errors, we recalculate w_i for each model performing the summation in the denominator of equation (3) across all models in the confidence set. The model weighted parameter estimates ($\hat{\theta}$) are then calculated using equation (4), where w_i is the recalculated model weight and $\hat{\theta}_i$ is the parameter estimate from the model; the product of these values is summed across all models (R) in the confidence set.

$$\widehat{\widehat{\theta}} = \sum_{i=1}^{R} w_i \times \widehat{\theta}_i \tag{4}$$

Standard error estimates that are not conditional on any one model are calculated using equation (5).

$$\widehat{se}\left(\widehat{\widehat{\theta}}\right) = \sum_{i=1}^{R} w_i \sqrt{\widehat{var}\left(\widehat{\theta_i} | g_i\right) + \left(\widehat{\theta_i} - \widehat{\overline{\theta}}\right)^2}$$
(5)

The term $\widehat{var}(\widehat{\theta_i}|g_i)$ represents the conditional variance of a parameter estimate under an individual model whereas $(\widehat{\theta_i} - \widehat{\overline{\theta}})^2$ is simply the squared deviation of the parameter estimate under a given model from the model weighted average for that parameter.

Our I-T approach also provides estimates of variable importance calculated by summing w_i of all models (*R*) in which a CGE occurs (eq. 6).

$$v_i = \sum_{i=1}^{R} w_i \tag{6}$$

The v_i score provides evidence that a CGE is important even if its contribution is small or poorly defined.

For the remainder of the article, we denote CGEs using a capital letter for the source of an effect: autosomal (A), cytotype (C), maternal effect (M), X chromosome (X), Y chromosome (Y); and we use lower case to denote the type of effect: additive (a) or dominance (d). Two-locus epistatic CGEs are denoted by joining the single locus notations (e.g., AaAd is autosomal additive by autosomal dominance epistasis).

INTERPRETING RESULTS OF AN I-T APPROACH TO LCA

Interpreting LCA results using an I-T approach involves consideration of a number of factors not present in the traditional J-S approach. In our experience, few LCA datasets strongly support a single model of genetic architecture, yet goodness-of-fit statistics and parameter estimates are typically only reported for the best model. A major advance of SAGA, and the I-T approach more generally, is the ability to quantify the degree of model selection uncertainty. In general, the lower the Akaike weight of the best model and or the more models contained in the 95% confidence set, the greater the degree of model selection uncertainty. Using our software, users can plot the distribution of Akaike weights across all possible models to allow a simple visual interpretation of model selection uncertainty.

In cases in which there is considerable model selection uncertainty, v_i scores often provide a strong indication of the importance of a specific CGE's role in the genetic architecture of a trait. This occurs because even when a 95% confidence set contains many models, one or a handful of CGEs may be present in the majority of them. In these situations, we can infer that the CGE is likely to be important, but we may have little confidence in estimating its true magnitude or sign because it depends on the other components in the model.

After assessing model selection uncertainty and v_i scores, we can evaluate the CGE estimates and their unconditional error estimates. Due to the inherent biases in previous J-S approaches noted above, our model-averaged parameter estimates will often be of lower magnitude and because the error now properly includes model selection uncertainty it will often be higher. SAGA returns a table containing the model-averaged parameter estimate and unconditional standard error for all CGEs included in the 95% confidence set of models.

VALIDATING THE I-T APPROACH

To evaluate our I-T approach to LCA, we created 1250 simulated datasets under five simulation conditions based on the sample sizes, midparent mean, and standard deviations observed in a study of sperm receptacle length in Drosophila mojavensis (Miller et al. 2003). The first four simulation conditions are based on a simple genetic architecture in which the midparent mean is 4.58 and there are three CGEs (Aa, Ma, AaAd) that each contribute to variation among line means with equal magnitude. The magnitude of each CGE was 0.25, 0.5, 1, and 2 in conditions 1 through 4, respectively, and 250 datasets were simulated under each of these conditions. Although the architecture is simple in all cases, by varying the magnitude of the CGEs we simulate data that pose difficulty for traditional approaches that must not only specify the best model but accurately estimate the values of the CGEs. We also generated an additional 250 datasets in which the true CGEs are expected to be difficult to estimate because the genetic architecture is complex. For these simulations the midparent mean is also 4.58, but six CGEs (Aa, Ad, Ma, AaAa, AaAd, AdAd) contribute to line means, all with magnitude = 1. For each simulated dataset, we included the following mixed sex cohorts: P1, P2, F1 $(P1 \times P2)$, rF1 $(P2 \times P1)$, $(P1 \times F1)$, $(rF1 \times P1)$, $(P2 \times F1)$, $(rF1 \times P2)$; parents are indicated as sire \times dam. We introduced sampling error to the simulated cohort means by randomly sampling 30 values from a normal distribution centered on the known cohort mean (specified by model parameters), and a standard deviation equal to 0.087 (the highest standard deviation recorded in the D. mojavensis dataset). The CGEs that we can evaluate with these cohorts are as follows: Aa, Ad, Ca, Ma, Md, AaAa, AaAd, AdAd, CaAa, and CaAd. These 10 effects allow for more than 800 possible underlying models.

We also compare the results of our I-T approach to the results from Miller et al. (2003), and our own LCA of hybrids among *Tribolium castaneum* populations (Demuth and Wade 2007a,b) and *Silene* species (Demuth et al. 2014). The LCA of coevolution between male sperm length and female sperm receptacle length (empirical datasets 1 and 2, respectively) among populations of *D. mojavensis* (Miller et al. 2003) was included because it is one of the few studies in which the authors published the underlying data for sexed cohorts. Analyzing the sexes separately allows us to include sex chromosome effects, which greatly expands the potential model space. This increase in model space is a problem for traditional LCA approaches, but less so for the I-T approach in SAGA.

From previous work by Demuth and colleagues, we reanalyze the genetic architecture of divergence among a cosmopolitan sample of T. castaneum interpopulation crosses (empirical datasets 3-17). We include 15 population pairs in which the number of offspring was measured, based on the original analysis, we expect to harbor a wide range of genetic architectures. We also reanalyze the recent LCA of interspecific hybrids between S. latifolia and S. diclinus (Demuth et al. 2014). This study analyzed male and female fertility (ovule and pollen production) and viability (offspring number for each sex) in pure parental crosses and interspecific hybrids (empirical datasets 18-22); Table S2 provides detailed information on all empirical datasets. In all cases, the original studies implemented a J-S approach using X^2 to assess model fit and likelihood ratio tests to add or remove CGEs from the overall model; we contrast these to results with the I-T approach implemented in SAGA.

All analyses were computed using our software package SAGA version 1.0 loaded with RStudio version 0.98.976 running R version 3.02 on a MacBookPro with 4 GB of 2600 MHz RAM and a 2.5 GHz processor (RStudio 2012; R Development Core Team 2013). Our R package is available from the CRAN repository and includes a vignette (supplement text 1) that guides users through an analysis of two empirical datasets.

Results

SIMULATIONS STUDIES

To evaluate the performance of our I-T approach using simulated data, we report the accuracy of parameter estimates, as well as performance in identification of CGEs included in the generating model. In simulated datasets with simple architectures in which we varied the magnitude of CGEs, SAGA accurately estimated the true values in all cases (Fig. 1A-D). In fact, even when the magnitude of the CGEs was only 5% of the mean, the estimate of the magnitude of the CGEs was within 2% of the true value (Fig. 1A). A key benefit of SAGA is that the parameter estimates are accurate despite substantial overall model selection uncertainty. The true model used to generate the simulated data was only identified as the best model in 73, 71, 73, and 69% of the replicates among datasets simulated under conditions 1–4, respectively. The fact that SAGA very accurately estimates parameter

values while simultaneously failing to always identify the correct model as best is likely due to CGEs that have small parameter estimates, large standard errors, and low v_i but by chance explain enough stochastic variation in cohort means to be included in a subset of high scoring models.

Because analysis of the simple architecture with effect sizes of 2 (simulation condition 4) had the lowest success (69%) in identifying the generating model as best, we used it to investigate the impact of model misspecification on parameter estimates. We parsed the results from the 250 replicates based on whether the true generating model was identified as the best model (Fig. 1E; N = 174) or not (Fig. 1F; N = 76). Even in the 76 datasets in which the generating model was not identified as the best model, the individual parameter estimates remain accurate. There were no cases in which the estimates for CGEs excluded from the generating model were as large as the estimates for CGEs included in the generating model.

The last set of simulated data offers the opportunity to evaluate a more complex genetic architecture in which the number of CGEs generating the cohort means is approaching the maximum number of estimable parameters (8 cohorts - [6 CGEs + intercept] = 1 degree of freedom). Our analysis of these data shows that SAGA can clearly distinguish the CGEs generating the line means based on v_i scores. Table 1 shows the minimum v_i for a CGE included in the generating model was 0.659 whereas the maximum v_i for a CGE excluded from the generating model was 0.02. We find that most CGEs are accurately estimated. In particular, Aa, Ma, and AaAd have mean estimates of 0.994, 1.000, and 0.998, respectively, and v_i scores of 0.993, 0.997, and 0.996 respectively. The three other CGEs included in the generating model (Ad, AaAa, AdAd) have more variable estimates ranging from 0.663 to 1.173 due to a linear dependency between the CGEs that precludes their joint estimation with the cohorts simulated. Thus, the parameter estimates for Ad, AaAa, and AdAd are generated by fewer models (those that are missing at least one of the CGEs). Despite this, the parameter estimates and the v_i scores for these three CGEs are all at least one order of magnitude greater than the estimates for CGEs that were not included in the generating model (Table 1).

ANALYSIS OF EMPIRICAL DATA

Analysis of the 22 empirical datasets in SAGA revealed the anticipated advantages of using an I-T approach: (1) successfully finding complex models in which J-S fails; (2) providing a clear signal of model selection uncertainty; (3) identifying CGEs that are often ignored; and (4) providing parameter and error estimates unconditional on any single model. The results for all empirical datasets are reported in Table 2. Below we briefly report results from the analyses of several exemplar datasets that illustrate the range of model selection uncertainty we have found in empirical data.



Figure 1. Analysis of four simulated datasets with varying magnitude of CGE contribution. Each plot shows the distribution of model weighted parameter estimates from 250 replicates. In each the left most curve is for CGEs with a true value of 0, the middle curve is for CGEs that generated the line means, and the right most curve is for the estimate of the overall mean. In all cases, the generating model included Aa, Ma, and AaAd. Dashed lines indicate the generating parameter values. Effect sizes: A = 0.25, B = 0.5, C = 1, D = 2. Iterations that correctly (E) or incorrectly (F) identified the generating model are shown separately for simulations in which effect size is 2.

Analysis of female sperm receptacle length (empirical dataset 1) provides an example with low model selection uncertainty. Although no single model had a w_i sufficient to ignore model selection uncertainty (95% confidence set includes 82 models with the highest $w_i = 0.234$), two CGEs exhibit v_i scores much higher than any others. These two CGEs (Aa and CaXa) had the largest estimated magnitudes of 0.0324 ± 0.0615 and 0.214 ± 0.0787 and high v_i scores of 0.98 and 0.89, respectively. All other CGEs had parameter estimates at least sevenfold smaller and had standard errors overlapping zero (Fig. 2).

Analysis of male sperm length (empirical dataset 2) provides an example of intermediate model selection uncertainty. In this case, no single model was found to be best (95% confidence set includes 302 models with the highest $w_i = 0.154$). However, a clear signal from v_i scores suggests that Aa and CaYa are important contributors to line means (0.91 and 0.79 v_i scores, respectively). These two CGEs also had the largest estimated magnitudes of 0.0495 ± 0.0133 and 0.0420 ± 0.0184 (Fig. 3). Most other CGEs estimated for this dataset had either low v_i scores, or the effect size estimate was comparatively small -0.0123 ± 0.0077 . This is an example of the ability of the I-T approach to recover complex genetic architectures that were missed when a single best model was selected. The intermediate level of uncertainty in which no single model is defined as far superior (Table 2) but a clear signal as to which CGEs are important was the most common result in our empirical analyses, found in datasets 1–10, 12, and 14–22.

The LCA for crosses between *T. castaneum* populations from Malaysia and Croatia (empirical dataset 13) is an example in which we find relatively high model selection uncertainty. The 95% confidence set of models required the inclusion of 363 models and the highest $w_i = 0.034$ (Table 2). The v_i scores were also low, with the highest being assigned to Ca and CaAd both with

Variable	Variable importance	Estimate/true value	Unconditional SE
Mean	1.000	4.746/4.58	0.773
Aa	0.993	0.994/1.00	0.016
Ad	0.659	0.662/1.00	1.545
Ca	0.005	0.007/0.00	0.007
Ma	0.997	1.000/1.00	0.013
Md	0.005	0.000/0.00	0.005
AaAa	0.66	0.827/1.00	0.774
AaAd	0.996	0.998/1.00	0.035
AdAd	0.67	1.173/1.00	0.774
CaAa	0.02	0.007/0.00	0.004
CaAd	0.014	-0.007/0.00	0.003

Table 1. Mean variable importance (v_i) and parameter estimates for 250 datasets generated under simulation condition 5.

Bold lines indicate variables included in the generating model.



Figure 2. Model weighted parameter estimates for sperm receptacle length in *D. mojavensis*. Bars are colored based on v_i scores and indicate the magnitude of the genetic effects indicated on the x-axis. Whiskers indicate the unconditional standard errors.

scores of 0.43. Furthermore, the standard error of the estimates for all CGEs overlap zero (Fig. 4). This dataset illustrates that in some cases the degree of model selection uncertainty can be so high that LCA is not able to recover the genetic architecture of the trait of interest with the cohorts available. The only other empirical dataset in our analyses that showed a similar level of uncertainty was dataset 11, which contained 310 models in the 95% confidence set and all CGE estimates failed to exclude zero.

Finally, analyses of pollen production and male offspring number (empirical datasets 19 and 21; Table 2) in hybrids between *S. latifolia* and *S. diclinis* represent two examples in which there was extreme model uncertainty. Compared to the original J-S analyses these two datasets yielded the same and different estimates of genetic architecture respectively. The types of crosses in the *Silene* study were carefully chosen to maximize the number of CGEs that could be tested and consequently resulted in a model space of greater than 100,000 potential genetic architectures. The 95% confidence set of models for pollen production (empirical dataset 19) included 2524 models and the highest $w_i = 0.047$ (Table 2). Despite the high model uncertainty, the CGEs with highest v_i scores (AaAd and XaAa) were the same as those identified by the J-S approach and the effect size estimates from the two approaches were statistically indistinguishable. In contrast, analysis of male offspring number (empirical dataset 21), which also had very high model uncertainty (3650 models in the 95% confidence set with highest $w_i = 0.14$), did not identify the exact CGEs identified as significant using the "right" model from the J-S approach. The I-T and J-S approaches both identify Ad and AaYa as important, but with different effect size estimates. The I-T approach also identified AdAd, CaAa, and CaYa as important,

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Figure 3. Model weighted parameter estimates for the genetic architecture underlying sperm length in *D. mojavensis*. Bars are colored based on v_i scores and indicate the magnitude of the genetic effects indicated on the x-axis. Whiskers indicate the unconditional standard errors. Only CGEs with v_i of at least 0.15 are included.



Figure 4. Model weighted parameter estimates illustrating relatively high model selection uncertainty for the genetic architecture underlying reproductive isolation in crosses between *T. castaneum* populations from Malaysia and Croatia (empirical dataset 13). Bars are colored based on *v_i* scores and indicate the magnitude of the genetic effects indicated on the x-axis. Whiskers indicate the unconditional standard errors.

whereas J-S identified Ca, AaAa, XaAa, and Ya. This final example is a case in which J-S with a vast number of models that have similar fits to the data coupled with a complex genetic architecture simply gets it wrong. Fortunately, the I-T and J-S approaches converge when removing the crosses where male number was likely to be low due to sex chromosome segregation problems in their fathers (F2d and BC2b; see Demuth et al. 2014). The reduced dataset (empirical dataset 22) had modest model uncertainty (307 models, with highest $w_i = 0.11$) and both approaches identify AaAa, AaAd, and AdAd as the CGEs contributing to the genetic architecture.

SOFTWARE PERFORMANCE

All analyses attempted in our study were completed in reasonable times on a standard laptop described in the methods section. Evaluation of the 250 replicates of all of the simulated datasets required a total of 12 min. Due to the nature of memory usage in R, performance on the datasets that contain independent data for males and females was initially a concern because it allows for a far greater number of models. For instance, the analysis of sperm receptacle length in *D. mojavensis* females required evaluation of approximately 13,000 models, whereas the analysis of sperm length in *D. mojavensis* males required evaluation of 63,000



Figure 5. Visual depictions of model space for the genetic architecture of reproductive isolation in *T. castaneum*. Each box represents a genetic architecture model is colored to reflect its w_i . The scale ranges from lightest for models with w_i of zero to darkest for those with the maximum value for the analysis. Models are organized with the simplest model at the lower left and increase in complexity upward and to the left, that is, all one-parameter models are on the bottom row followed by two-parameter models when the right edge of the graph is reached a second row is added on top of the first. (A) Results from the analysis of dataset 4 showing low model selection uncertainty. (B) Results from the analysis of dataset 6 showing considerable model selection uncertainty.

models. These analyses required only 2 and 5 min, respectively, to complete. The most computationally intensive search among our analyses (*Silene* hybrid female number) required evaluation of 192,984 models and took 49 min.

Discussion

Comparing the original results from of all 22 empirical datasets with those from SAGA suggests that the I-T approach is more successful than traditional approaches at identifying higher order CGEs. For example, nine of the datasets had one or more epistatic CGE (11 in total) not identified with the J-S test that had a v_i > 0.5 in the I-T analysis. One datasets had maternal effects not identified with the J-S test that had $v_i > 0.5$ in the I-T analysis, and only one dataset had a nonepistatic autosomal CGE identified with the I-T approach but not with the J-S test. These results indicate that the traditional version of the J-S test may underestimate the contribution of epistatic interactions in determining phenotypes.

Finding a larger role for epistasis in empirical datasets is particularly important since, as highlighted in the introduction, it affects our perception of how adaptation and speciation are likely to occur in nature. For instance, if epistasis is a common feature of the genetic architecture of variation within species, then small variations in allele frequency among populations with limited gene flow may result in rapid genetic divergence among those populations even if selective pressures are similar (Goodnight 1987, 1988; Wade and Goodnight 1998). Because not all types of epistasis are equally disposed to fostering population divergence and or speciation (Demuth and Wade 2005), the methods developed in SAGA are especially important because they provide a much more powerful way to differentiate among all the components of complex genetic architectures. The utility of SAGA and LCA will be particularly powerful for systems in which there is a continuum of divergence among populations as well as species that are in the so called "Goldilocks zone" (Demuth et al. 2014) in which viable hybrids can still be produced. In such systems LCA allows for the investigation of how architectures change as traits diverge and reproductive isolation arises between species.

There has been concern that comparing the large number of possible models in LCA experiments may lead to spurious results (Bieri and Kawecki 2003). This concern seems to trace back to discussions of "data dredging" (Burnham and Andersen 1998; Burnham and Anderson 2002). Described in the context of ecological studies, data dredging is the process of measuring and searching for significance among a great many variables without a clear a priori decision of what variables may be biologically important. Burnham and Anderson encourage careful selection of a reduced set of variables based on a sound understanding of the biology involved and by doing this reducing the total number of models that must be evaluated (2002). In LCA, the variables are known CGEs, and each one describes a biologically plausible component of the genetic architecture underlying the phenotypes of the observed cohorts. The goal of LCA, finding the set of CGEs that best explains the observed data, can best be accomplished if we examine all possible combinations of CGEs. Assuming the necessary cohorts are available, the I-T approach accomplishes this goal.

Existing approaches to LCA share two common shortcomings: (1) there is no framework to adequately describe model selection uncertainty, and (2) there is no way to quantify the impact of model uncertainty on the estimated contributions of individual CGEs. The importance of model selection uncertainty is highlighted by our analysis of empirical data in which 21 of 22 datasets showed nontrivial model selection uncertainty. The ability to quantify model selection uncertainty is perhaps one of the most important benefits of turning to an I-T approach. Previous analyses (even those that implemented AIC to choose a model) have presented only results conditional on specific models, and have largely ignored uncertainty in model selection. Furthermore, hypothesis-testing approaches do not provide us with a way to rank models relative to one another. For instance the result of the J-S approach cannot tell us if one or many models are almost as good as the best model identified. Akaike weights and evidence ratios offer a natural way to do this.

The maximum w_i of all models tested as well as the number of models required to produce a 95% confidence set are two simple metrics that quantify the degree of uncertainty in model selection. The maximum w_i we recorded ranged from 0.02 to 0.98 with a mean maximum $w_i = 0.21$. The number of models required to construct a 95% confidence model set varied accordingly, ranging from 82 in the case of sperm receptacle length in *D. mojavensis* (dataset 1) to 5385 models for the number of females produced in crosses between species of *Silene* (dataset 20, Table 2). We illustrate examples in which model selection uncertainty is low (dataset 4; Fig. 5A) and high (dataset 6; Fig. 5B). The model uncertainty metrics and visual depiction of model space allow for a more realistic interpretation of LCA experiments than previous approaches.

By implementing an I-T approach and examining all models possible given the data, we also resolve the issue of finding the best possible model. The potential of failing to find the best model was illustrated in our analysis of dataset 1 in which we found a model that outperformed all other possible models that the J-S test had failed to find. However, the ultimate goal of LCA is to find the composite genetic effects responsible for a phenotype. Previous methods depend on identifying the best model and interpreting the CGEs that are included in that model (conditional effects). With SAGA we get accurate estimates of the CGEs that are not dependent on the ability to specify one overall model as best, and our analysis of simulated datasets indicates that even when we are unable to identify the generating model our I-T approach is still able to identify the generating CGEs. The I-T approach to LCA we have presented eliminates issues in existing approaches and offers a more powerful and nuanced examination of the genetic architecture of quantitative traits. Furthermore, estimates of CGEs are unbiased and confidence intervals incorporate model selection uncertainty, a characteristic impossible under previous

approaches. Finally, the ability to visualize the distribution of Akaike weights of all possible models can provide a strong indication of whether LCA of the phenotype of interest is informative. We recommend that future studies assess model uncertainty and shift away from making estimates that are conditional on a single model.

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Supporting Information

Additional Supporting Information may be found in the online version of this article at the publisher's website:

 Table S1. Matrix of composite genetic effects included in SAGA.

 Table S2. Detailed information on the identity of crosses reanalyzed.